

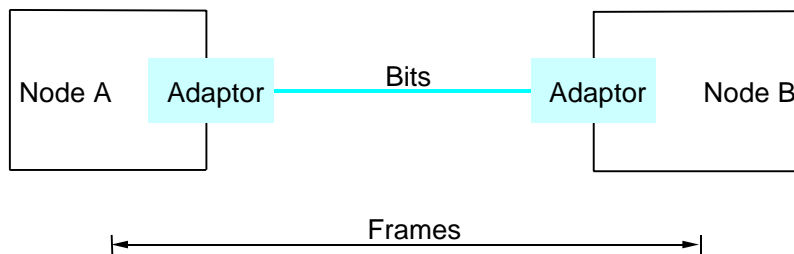
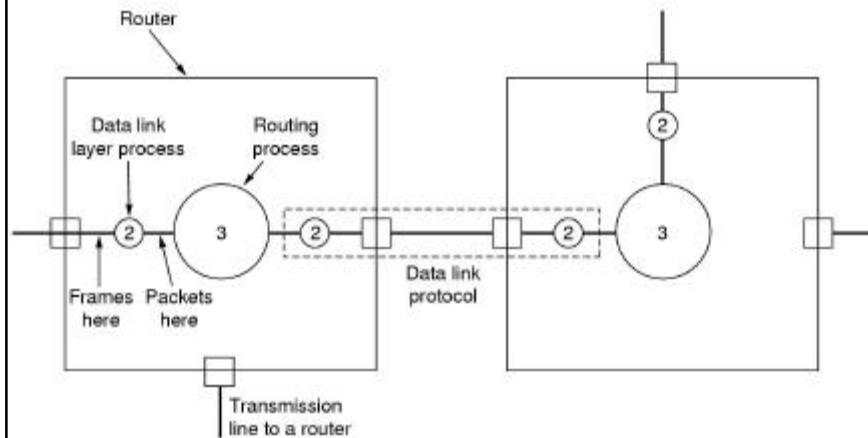
# Computer Networks

## The Data Link Layer

## Data Link Layer

- Framing
  - Byte oriented protocols (e.g. IBM BISYNC, ARPANET IMP-IMP, DEC DDCMP)
  - Bit oriented protocols (e.g. IBM SDLC, ISO HDLC, CCITT X.25 LAPB)
  - Clock-based (TDM, SONET)
- Error Detection & Correction: Parity checking, CRC, Hamming codes
- Flow Control & Reliable Transmission
  - Stop-and-wait
  - Sliding Window
    - go-back-n
    - selective repeat

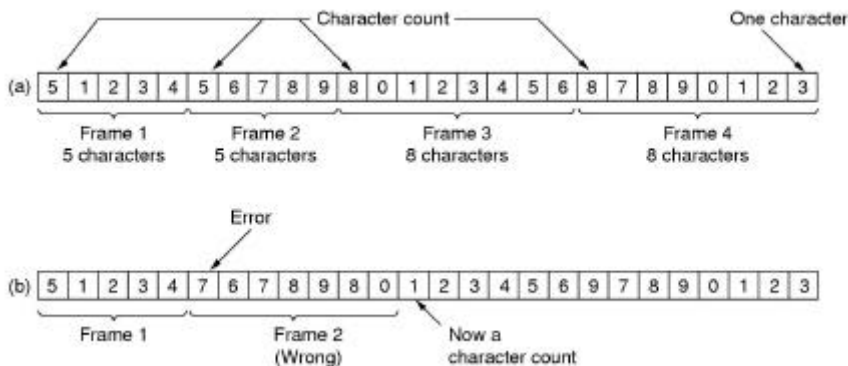
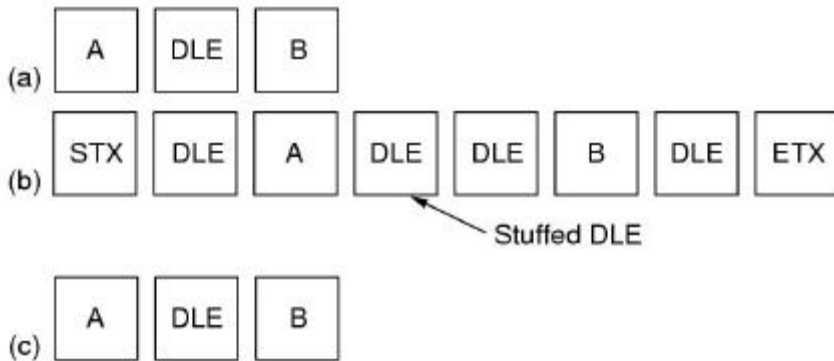
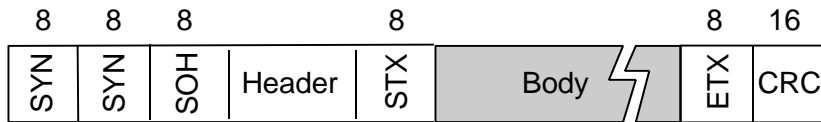
# The Data Link Layer



# Byte Oriented Protocols

- Sentinel Approach (IBM's BISYNC, ARPANET's IMP-IMP):
  - Enclose packet in special sentinel characters:
    - SOH-STX-ETX for BISYNC: need to escape ETX, variable header
    - DLE/STX-DLE/ETX for IMP-IMP: escape DLE
  - Problem with corruption of sentinel characters
- Byte Counting (DECNET's DDCMP):
  - include number of bytes (COUNT) in header
  - Problem with corruption of COUNT field
- Disadvantage of Byte oriented Protocols: tightly tied to character codes

# Byte Oriented Protocols



# Bit Oriented Protocols

- Variable length bit streams
- Sender:
  - encloses packet (bit stream) : 01111110
  - appends a 0 after each 1111 in body (*bit stuffing*).
- Receiver, upon receiving 011111:
  - next bit 0: stuffed bit is removed
  - next bit 1:
    - if next bit 0 (i.e. 01111110): end of frame marker
    - if next bit 1 (i.e. 01111111): error

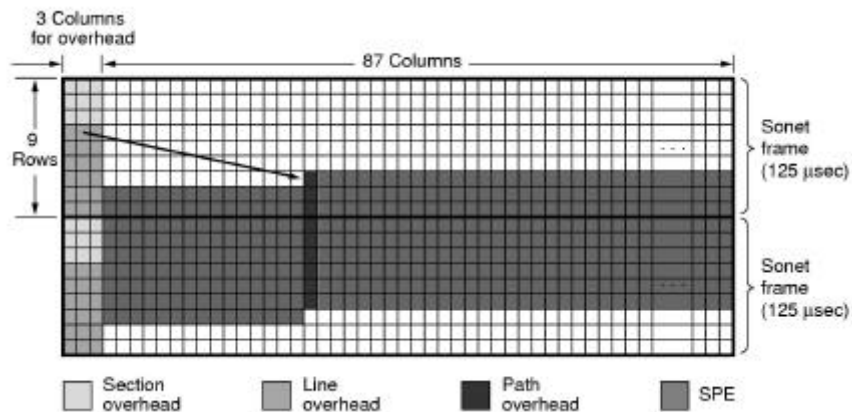
(a) 0 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 1 0

(b) 0 1 1 0 1 1 1 1 1 0 1 1 1 1 1 1 0 1 1 1 1 1 0 1 0 0 1 0

Stuffed bits

(c) 0 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 1 0

# Clock-based Protocols (e.g. SONET)



# Parity Checking

- One additional bit to make number of 1's even (or odd)
  - Detection of odd (even) bit errors: even (odd) number of errors are not detected (50% of burst errors)
- Two additional bits for even and odd numbered bits
  - Detection of single or even/odd pair bits
- Burst error detection
  - Basic idea: Distribute the bits of a message in different frames
  - Guaranteed to detect errors due to bursts whose duration is less than the time to send one frame
  - Detects longer burst errors with probability  $1 - (1/2)^n$

# Parity Checking

Figure 4.1 Detecting Single Bit Errors Using Parity Checking

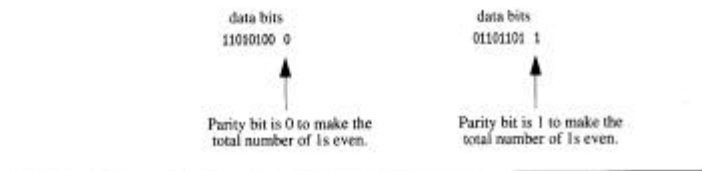


Figure 4.2 Detecting Consecutive Double-Bit Errors Using Parity Checking

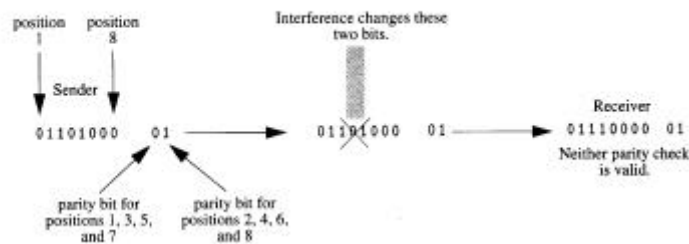


Figure 4.3 Detecting Burst Errors Using Parity Bits

| Sender             |                        |   | Receiver      |                        |    |
|--------------------|------------------------|---|---------------|------------------------|----|
| Row (frame) number | Parity bit for one row |   | Row number    | Parity bit for one row |    |
| 1                  | 01101                  | 1 | 1             | 01101                  | 1  |
| 2                  | 10001                  | 0 | 2             | 10001                  | 0  |
| 3                  | 01110                  | 1 | 3             | 01100                  | 1* |
| 4                  | 11001                  | 1 | 4             | 11001                  | 1  |
| 5                  | 01010                  | 0 | 5             | 01000                  | 0* |
| 6                  | 10111                  | 0 | 6             | 10101                  | 0* |
| 7                  | 01100                  | 0 | 7             | 01100                  | 0  |
| 8                  | 00111                  | 1 | 8             | 00101                  | 1* |
| 9                  | 10011                  | 1 | 9             | 10001                  | 1* |
| 10                 | 11000                  | 0 | 10            | 11000                  | 0  |
| Column number      | 12345                  | 6 | Column number | 12345                  | 6  |

Burst error occurs and destroys column four, making it all zeroes.

\* Parity bit is not correct

# Cyclic Redundancy Checks

- Based on polynomial division
  - $b_n b_{n-1} b_{n-2} \dots b_1 b_0 \rightarrow b_n x^n + b_{n-1} x^{n-1} + b_{n-2} x^{n-2} + \dots + b_1 x^1 + b_0$
- Steps:
  - Given a bit string B, append a number (= degree of G(x)) of 0s to the end of it: B(x)
  - Divide B(x) by a agreed-on generator polynomial G(x) and get the remainder R(x)
  - Define T(x) = B(x) - R(x). (note: T(x)/G(x) generates a 0 remainder)
  - Transmit T → T(x) which will arrive as T'(x).
    - If T'(x)/G(x) generates a 0 remainder OK. Otherwise error!

## CRC Analysis (I)

- On what conditions  $T'(x)/G(x)$  will yield a 0 remainder?
  - Changing  $T(x)$  is like adding to it an unknown  $E(x)$ :  
$$T'(x) = T(x) + E(x) \Rightarrow T'(x)/G(x) = [T(x) + E(x)]/G(x) = T(x)/G(x) + E(x)/G(x)$$
  - Undetected transmission errors correspond to errors for which  $G(x)$  is a factor of  $E(x)$ 
    - If  $G(x)$  has at least 2 terms all single-bit errors are detected
    - If  $x$  is not a factor of  $G(x)$  then all burst errors having length  $\leq$  to the degree of  $G(x)$  are detected.
    - If  $x+1$  is a factor of  $G(x)$ , then all burst errors damaging an odd number of bits are detected
    - ...

## CRC Analysis (II)

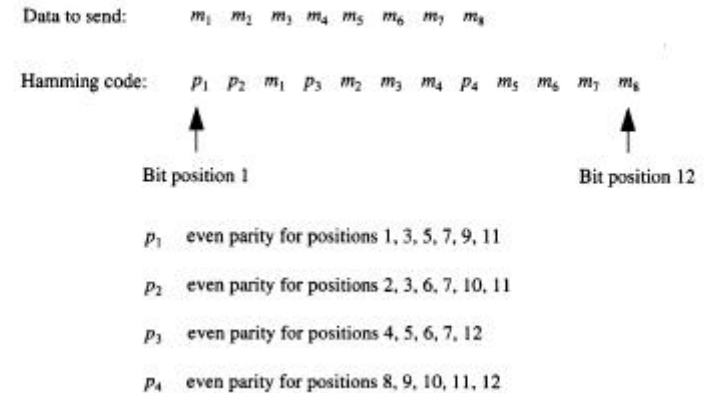
- If  $x$  is not a factor but  $x=1$  is a factor then CRC detects:
  - all burst errors of length  $r <$  degree of  $G(x)$
  - all burst errors affecting an odd number of bits
  - all burst errors of length  $r+1$ , with probability  $(2^{r-1}-1)/2^{r-1}$
  - All burst errors of length  $> r+1$  with probability  $(2^r-1)/2^r$
- Typical  $G(x)$  polynomials:
  - CRC-12:  $x^{12} + x^{11} + x^3 + x^2 + x + 1$
  - CRC-16:  $x^{16} + x^{15} + x^2 + 1$
  - CRC-CCITT:  $x^{16} + x^{12} + x^5 + 1$
  - CRC-32:  $x^{32} + x^{26} + x^{23} + x^{22} + x^{16} + x^{12} + x^{11} + x^{10} + x^8 + x^7 + x^5 + x^4 + x^2 + x + 1$

# Hamming Codes

- Based on the concept of Hamming distance: the number of bit positions in which 2 bit strings differ
- Error correcting code
- Uses  $r$  parity bits to detect and correct single bit errors: for  $m$  data bits,  $m+r+1 \leq 2^r$ 
  - parity bits are placed in positions  $k$ :  
 $k=2^i, i=0,1,2,\dots$
  - (data/parity) bit in position  $k$  contributes to the parity bits in positions  $i$  where:  
 $k = \sum_{i=2^x} i, i=2^x$
  - Inverted bit is in position  $i$ , where  
 $i = \sum_{k=position\ of\ parity\ bit\ with\ wrong\ value}^x k$
- Burst errors as in simple parity

# Hamming Codes

FIGURE 4.9 Hamming Code for Single-Bit Error Correction



# Hamming Codes

FIGURE 4.10 Bit Stream Before Transmission

Data: 0 1 1 0 0 1 1 1  
 $m_1$   $m_2$   $m_3$   $m_4$   $m_5$   $m_6$   $m_7$   $m_8$

Hamming code: 0 1 0 1 1 1 0 1 0 1 1 1  
 $p_1$   $p_2$   $m_1$   $p_3$   $m_2$   $m_3$   $m_4$   $p_4$   $m_5$   $m_6$   $m_7$   $m_8$

FIGURE 4.11 Parity Checks of Frame After Transmission



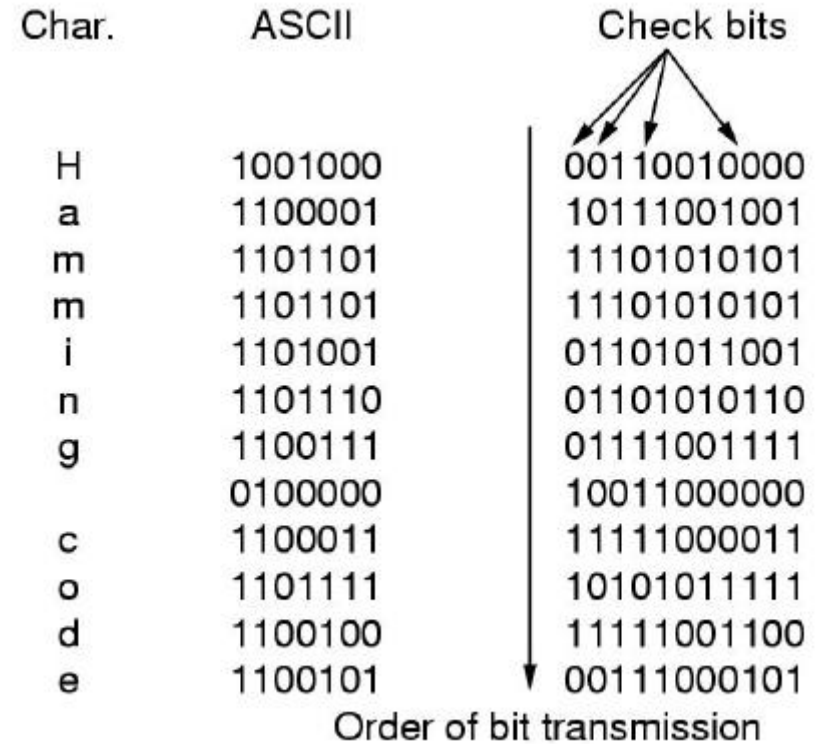
- Indicates bits checked using  $p_1$ ; parity check fails. 1
- ▲ Indicates bits checked using  $p_2$ ; parity check succeeds. 9
- Indicates bits checked using  $p_3$ ; parity check fails. 1
- ▭ Indicates bits checked using  $p_4$ ; parity check succeeds. 9

Error is in position  $1101 = 5$

TABLE 4.2 Bit Position Errors and Associated Parity Errors

| ERRONEOUS BIT POSITION | INVALID PARITY CHECKS   | $p_1 p_2 p_3 p_4$ |
|------------------------|-------------------------|-------------------|
| no error               | none                    | 0000              |
| 1                      | $p_1$                   | 0001              |
| 2                      | $p_2$                   | 0010              |
| 3                      | $p_1$ and $p_2$         | 0011              |
| 4                      | $p_3$                   | 0100              |
| 5                      | $p_1$ and $p_3$         | 0101              |
| 6                      | $p_2$ and $p_3$         | 0110              |
| 7                      | $p_1$ , $p_2$ and $p_3$ | 0111              |
| 8                      | $p_4$                   | 1000              |
| 9                      | $p_1$ and $p_4$         | 1001              |
| 10                     | $p_2$ and $p_4$         | 1010              |
| 11                     | $p_1$ , $p_2$ and $p_4$ | 1011              |
| 12                     | $p_3$ and $p_4$         | 1100              |

# Hamming Codes





# Flow Control

FIGURE 5.1 Flow Control Using Signaling

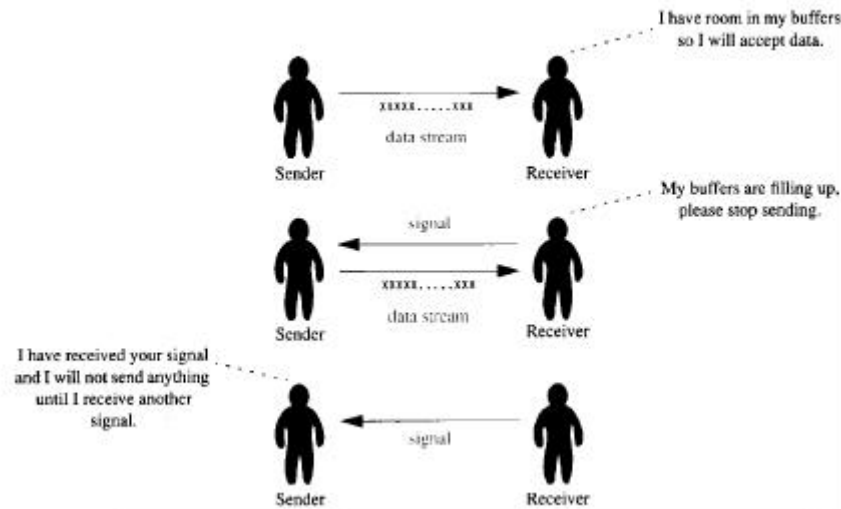
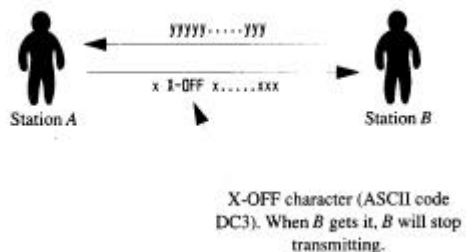


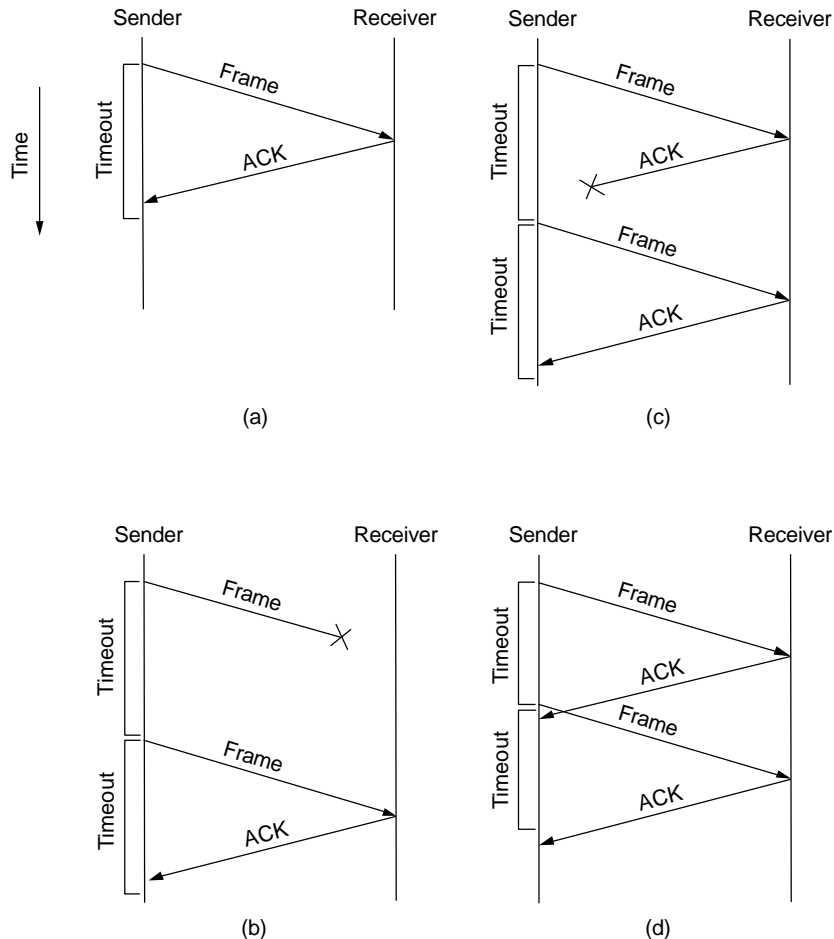
FIGURE 5.2 Flow Control Using Inband Signaling



# Stop-and-Wait

- Receiver acknowledges each frame
- Sender waits for ack before it sends the next frame
- Disadvantages: Poor efficiency
  - delay \* bandwidth: (delay = RTT or RTT/2)
  - channel utilization:
    - the percentage of time the channel is transmitting data frames
  - effective data rate:
    - The actual number of data bits sent per unit of time.
- *Exercise: Derive formulas for the above 2 metrics for the stop-and-wait protocol*

# Stop-and-Wait



# Sliding Window: go-back-n

- Sender assigns consecutive (modulo  $2^k$ ) sequence numbers to each frame: 0 to  $2^k - 1$
- **Sender maintains window** buffer of size  $2^k - 2$  (why?).
  - Everytime a frame is sent, it is buffered.
  - Frames are removed as they are acknowledged
  - If frame not acknowledged it is retransmitted **along with all outstanding frames** (go-back-n)
- Receiver expects to receive frames in order (modulo  $2^k$ ):
  - If frame is damaged **or out of order** it is discarded
- Receiver does not acknowledge each received frame explicitly. Ack piggybacks data frames and **refers to the most recently received frame**. Ack timeouts if no data.

# go-back-n

FIGURE 5.7 A Sliding Window Protocol

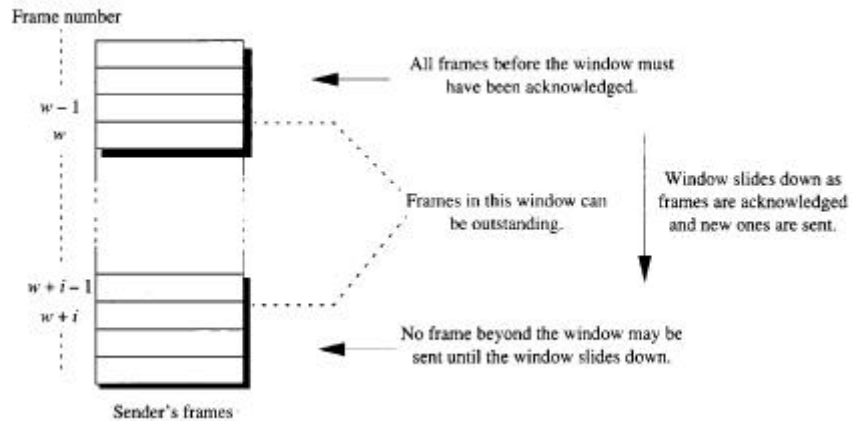


FIGURE 5.9 Typical Frame Format



# go-back-n

FIGURE 5.10 Protocol Failure When Window Size Equals 2<sup>n</sup>

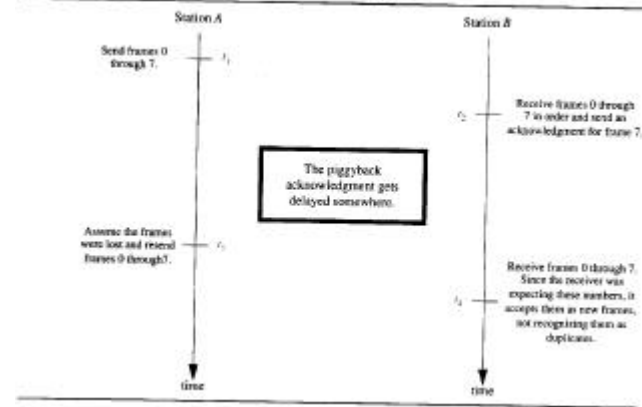
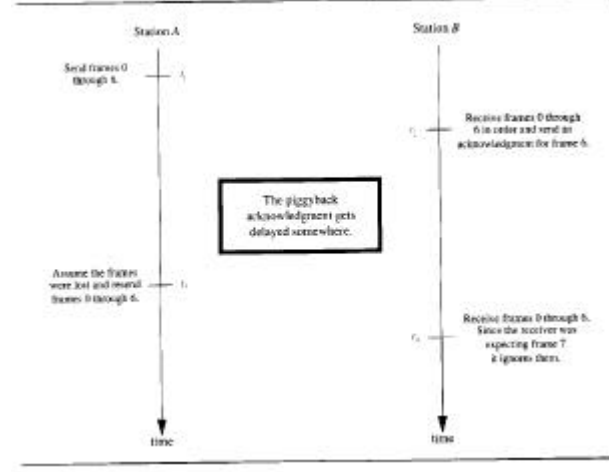


FIGURE 5.11 Protocol Success When Window Size Equals 2<sup>n</sup> - 1

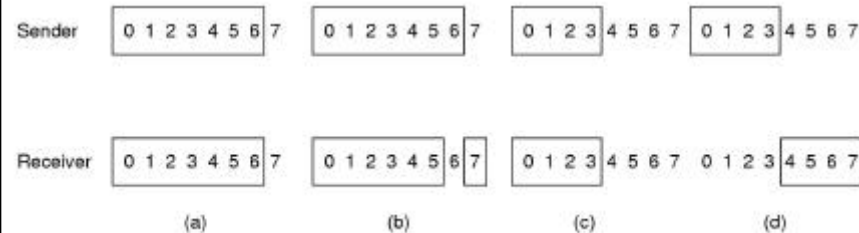
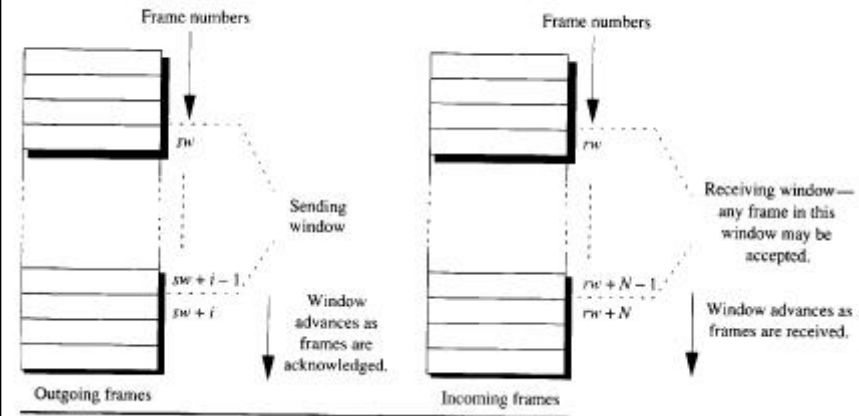


# Sliding Window: Selective Repeat

- Similar to go-back-n **but**:
  - Receiver
    - Utilises **window too**, which defines which frames can be received
    - Out of order frames that are in window are buffered even if they are out of order
    - Nack sent for damaged or delayed expected frame
    - Ack sent for frame  $f_i$ , where  $i$  is the largest sequence number such as all frames  $f_j, j < i$  have been received
  - Sender
    - Retransmits only timed out and Nack-ed frames
- Window sizes  $w$ :
  - $w_{sender} + w_{receiver} \leq 2^k$

# Selective Repeat

FIGURE 5.13 Sending and Receiving Windows for Selective Repeat Protocol



# Selective Repeat

FIGURE 5.14 Protocol Failure: Receiving Window Size is Greater Than  $2^k - 1$

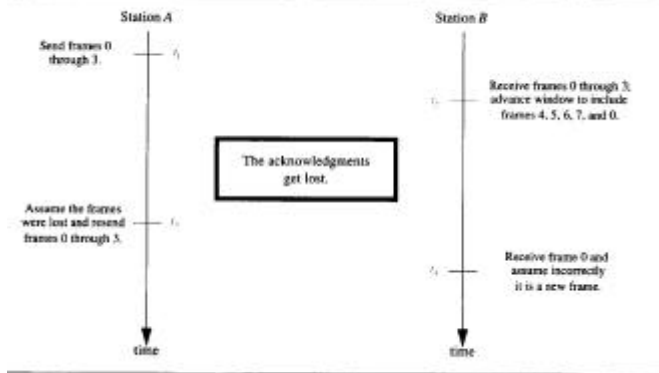
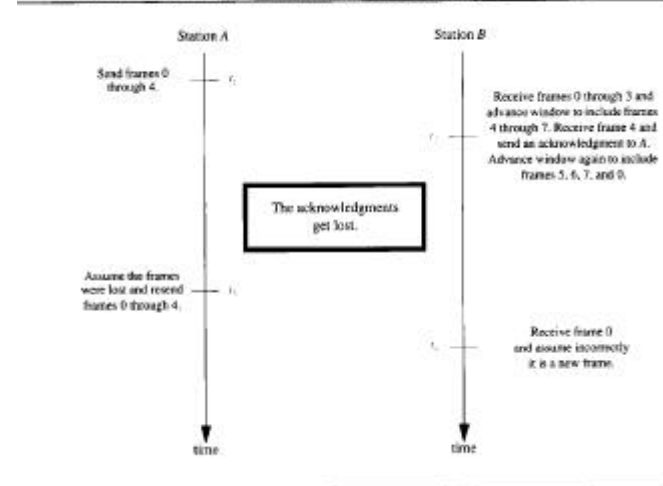
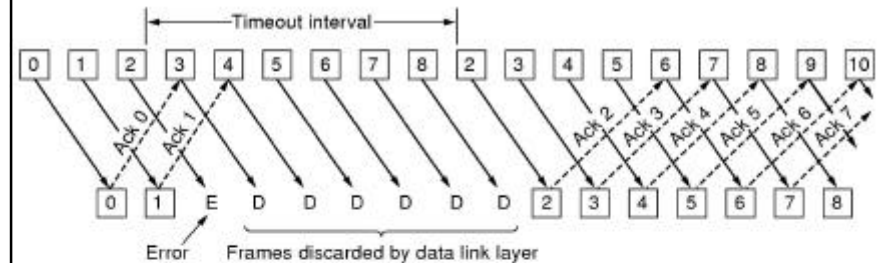


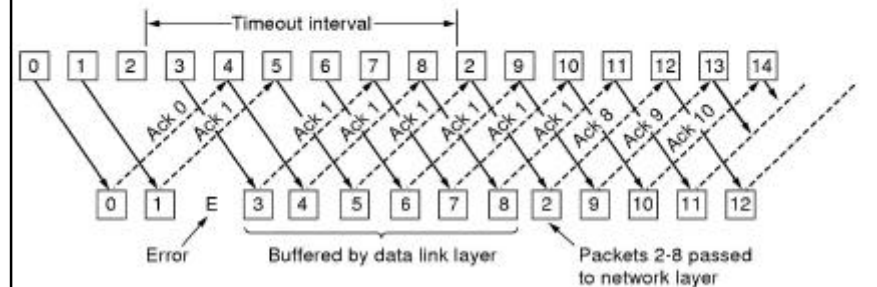
FIGURE 5.15 Protocol Failure: Sending Window Size is Greater Than  $2^k - 1$



# go-back-n vs Selective Repeat



(a)



(b)